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# A satellite view of internal waves induced by the Indian Ocean tsunami

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At 08:45 local time (02:45 GMT) on 26 December 2004, one hour and 45 minutes after the Sumatra Earthquakes of magnitude 9.3, a devastating tsunami struck the east coast of Sri Lanka. Nearly two hours and 30 minutes after the wave hit the coast, a weather satellite passed over Sri Lanka's coastal zone providing a rare glimpse of internal waves along the continental slope due to this tsunami. The satellite imagery indicates wavelike features from the tsunami being reflected, diffracted, and scattered off the steep continental slope and submarine canyons adjacent to Sri Lanka. The energetic wave and its modification to internal waves possibly eroded sediment from the sea floor and transported it to the sea surface. Solitary features generated by internal waves can explain the observed pattern. Future modelling approaches considering these non-linear interactions would be required for a better understanding of the tsunami behaviour in the coastal zone, where its destructive effects are most prominent.

Keywords: Tsunami; Internal waves; Suspended sediment; Remote sensing; MODIS

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## **1. Introduction**

The east coast of Sri Lanka comprises the SE part of the Bay of Bengal, located in the northeastern part of the Indian Ocean. The water depth in the Bay of Bengal varies between 10 m in the shelf area of Bangladesh to more than 4500 m at the Equator with by far the largest deep-sea fan of the earth. Its sedimentary infill is largely terrigeneous material derived from the Himalayas and transported through the Ganges-Brahmaputra Rivers into the northern Indian Ocean. The continental slope near the east coast of Sri Lanka is one of the world's steepest bathymetric features with several submarine canyons exceeding 45° in some locations. The geology of the shelf near Batticaloa at the coast of Sri Lanka encompasses coral reefs and sandy clay over gravel (IIOE 1964). The stratified water masses of the Sri Lanka east coast represent the low-salinity portion of the northern Indian Ocean caused by the high seasonally varying river run-off and precipitation contrary to the high-salinity waters of the Arabian Sea. As the Bay of Bengal is a part of the northern Indian Ocean, the oceanic circulation is controlled through the seasonally changing monsoon gyre (anti-clockwise through the Winter Monsoon current). Superimposed on this circulation are planetary mode waves (Eigenherr and Quadfasel 1999) and interannual variations related to the El Nino Southern Oscillation (Srinivas et al. 2005), which influences the concentration of nutrients and hence organic matter at the sea surface (Kumar and Ramesh 2005). During the NE monsoon the current velocities south of Sri Lanka are the strongest of the whole Indian Ocean and may exceed 1.8 m s<sup>-1</sup> (Wyrtki 1973). With lower nutrient concentrations offshore, pigment concentrations of phytoplankton decrease from the shelf region of Sri Lanka in the offshore direction.

Tsunamis are assumed to be long-period surface gravity waves triggered by coastal earthquakes, landslides, or volcanoes that obey, with their high energy, the generalized equations of phase speed  $c_s$  and group speed  $c_g$  for waves (LeBlond and Mysak 1978)

$$c_s = \sqrt{\frac{g}{k} \tanh(kH)} \tag{1}$$

$$c_{g} = \frac{c_{s}}{2} \left[ 1 + \frac{2kH}{\sinh 2kH} \right]$$
(2).

For tsunamis, eq. (1) and (2) can be approximated with  $kH \ll 1$  to  $c_s = \sqrt{gH}$  and  $c_s = c_g$  where k is the wave number, g the acceleration due to gravity, and H the depth of the water. In this assumption, the wave speed is non-dispersive (does not depend on the wave length) and a single frequency applies. Thus, the speed of the wave can be estimated if the depth of the ocean sea floor is known. The tsunami travelled in the Indian Ocean where the depth is about 4000 m, giving it a phase speed of about 200 m s<sup>-1</sup>. An initial wave length of ~500 km and change in sea level of about 70 cm has been detected from Jason 1 altimeter satellite (Gower 2005). When the wave approached the continental slope of Sri Lanka, parts of it were transmitted, reflected, and scattered and possibly generated internal waves. The tsunami likely generated suspended sediment (Pennish 2005) on the upslope and shallow water (McCave 2003) and transported finer sediment compositions to near the surface.

Internal solitary waves are generated by non-linear deformation of long waves like internal tides or tsunamis. They are a widespread and prominent feature in the oceans (Osborne and Burch 1980) and lakes (Farmer 1978) and are commonly associated with density-stratification. For example, satellite images off Gibraltar (Da Silva *et al.* 1998) reveal their distribution and propagation by an alteration of the sea surface roughness formed by a surface-internal wave current interaction of some type, sometimes modified by suspended matter, but the generation mechanisms are still controversially discussed (e.g. Nittrouer and Wright, 1988, Cacchione and Clark, 1990, Farmer and Armi 1999, Cacchione *et al.* 2002, Small 2001a,b). Internal solitary waves occur particularly near regions of variable bathymetry, such as shelf edges, seamounts, sills, and submarine canyons, where the bathymetry forces the pycnocline to oscillate with the frequency of the tidal wave or tsunami. Such conditions apply to the coast of Sri Lanka (Quadfasel 1998).

In this paper, we analyse remote sensing features in the region of Batticaloa on the eastern coast of Sri Lanka where the tsunami, with wave heights of 4-7 m, caused several thousand fatalities and injuries (Liu *et al.* 2005).

## 2. Data and Methodology

The National Aeronautics and Space Administration's (NASA) research satellite, Terra, a polar orbiting satellite carrying the Moderate Resolution Imaging Spectroradiometer (MODIS) instrument, passed over Sri Lanka on the morning of 26 December 2004. The MODIS instrument is a 36 channel imager consisting of visible/near infrared (VNIR) channels at 250 m and 500 m resolution and thermal infrared (TIR) at 1 km resolution at nadir. The instrument is designed for multi-discipline research, with sensors in spectral bands for atmosphere, ocean, and land interests. The spectral range in the VNIR wavelengths is 0.4 to 2.1 µm and in the TIR, 3.6 to 14.3 µm (Barnes *et al.* 1998). The data, in Level 1B format, were retrieved from the Goddard Earth Sciences Distributed Active Archive Center. The Level 1B format provides geolocated and calibrated radiances in the original satellite perspective. The calibration procedure to convert

sensor-output digital numbers to reflected radiance for the VNIR bands and thermally emitted radiance for the TIR bands is described in Guenther *et al.* (1998). An inverse Planck function is used to convert TIR emitted radiances to brightness temperatures (Petty 2004).

Figure 1 depicts a true colour MODIS image of this pass by colour-combining spectral band 1 (620 - 670 nm), band 4 (545 - 565 nm), and band 3 (459 - 479 nm), corresponding to red, green, and blue wavelengths. The MODIS instrument is capable of detecting significant disturbances in the sea by changes in the reflectivity of the water column (figure 2).

## 3. Results and Discussion

The left panel of figure 2 shows the reflectivity in the coastal zone before the perturbation of the tsunami (19 December 2004, 0510 GMT). High reflectance on the shelf is likely associated with suspended sediment by wind-induced wave-disturbances. The reflectivity is also affected by biological activity such as phytoplankton and zooplankton (Curran and Novo 1988) and subsurface plankton blooms have been identified during past surveys of the shelf (e.g. during the International Indian Ocean Expedition, 1964). In contrast to the relatively undisturbed case, the right panel shows the situation for 26 December 2004, 0515 GMT or about 2 hours and 30 minutes after the tsunami hit the shore of the east coast of Sri Lanka. Additional remote sensing data for other times were influenced by strong cloud coverage because of Sri Lanka's close proximity to the Intertropical Convergence Zone (ITCZ).

The features in figure 2 are likely generated by an internal wave due to the tsunami which itself was reflected, diffracted, and scattered off the continental slope.

Two types of waves can be seen in figure 2: linear and bow waves. These wave patterns match well the strong bathymetric gradient. The linear wave features are likely generated by reflection, near the straight continental slope, while bow waves can be created on canyons or sea mounts.

Figure 3 shows the high-gradient bathymetry region overlaid on the wave image. This region is 25 km wide where the ocean depth decreases from 3000 m to 50 m, moving from east to west. The reflected waves emanate from the left side of the highgradient region, which is the shelf break. Several submarine canyons adjacent to the shelf off the coast of Sri Lanka had been identified during the International Indian Ocean Expedition and measured to depths of 1000 to 1500 m. Interestingly, the measured wave length between the peaks of high reflectivity is about 6 km which would be far too short for the period (~40 minutes) and shallow water equation (1). According to analytic theories of tsunamis, the wave characteristics change substantially if they are scattered and reflected by a bathymetric feature like a steep continental slope, submarine canyons, or seamount (Mofjeld et al. 2000). Internal waves at surfaces between different density layers can be created by a tsunami pushing on the continental slope. The currents resulting from the internal waves interact with wind-generated surface waves to produce alternate bands of rough and calm water that are visible from space (Garret 2003). For long internal waves, the phase wave speed (eq. 1) modifies to  $c_s = \sqrt{g' h_1}$  with reduced gravity  $g' = g \Delta \rho / \rho_1$ , density difference between the two density layers  $\Delta \rho$  and density of the upper layer  $\rho_1$ . For  $\Delta \rho = 5 \text{ kg m}^{-3} \rho_1 = 1021 \text{ kg m}^{-3}$  (see BENGALWOCE, Quadfasel 1998) and h<sub>1</sub>=150m for the surface layer, the computed wavelength of the internal wave (6.4 km) is close to the 6 km wavelength shown on the MODIS image in figure 2. Over bathymetric features, internal waves may change

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currents, create a collapse of the mixed layer, and generate solitary wave patterns (Farmer and Armi 1999). Low-frequency internal waves are reflected off the sloping bottom toward the open ocean while internal waves with frequencies  $\omega > [(f^2 + N^2\alpha^2/(1+\alpha^2)]^{1/2}$  are deflected towards the head of canyons (Hotchkiss and Wunsch 1982). f is the Coriolis parameter, N the buoyancy frequency and  $\alpha$  the slope of the canyon bottom axis. The energy of these reflected waves points approximately in the direction of the local gravity vector (LeBlond and Mysak 1978, Cacchione *et al.* 2002). Curvature of the wavefront, as seen in the MODIS images, is potentially related to refractions of rays by variations in the water depth, nonlinear wave interactions, and stratifications (Small 2001a,b). Shallowing of the wave affects refraction because the phase speed of a nonlinear internal wave generating patterns similar to images from the MODIS instrument (figures 1-3).

Takayama and Saito (1999) proposed that tsunamis with their high speed in the deep ocean may be treated as quasi-supersonic waves. Patterns of such a shock wave and Mach reflection of shallow water waves (Toro *et al.* 2004) are significantly different from those of a traditional shallow water wave with concentrated interferences by the reflected waves, and could potentially alter the surface roughness as well.

In addition, the processes associated with particle transport and suspended material at the sea surface might be important to explain the MODIS images. Suspended matter in surface waters near the shelf break is related to biological processes, fluvial input from the shoreline, and upwelling of suspended sediment from the shelf and slope. There are two modes of sediment transport across the continental shelf (Cacchione and Drake 1990): 1. Bed load, in which individual grains collide, roll or saltate in the thin bottom boundary layer, and 2. Suspended load, in which the particles are advected with ambient currents. Increased particulate transport by strong shear currents in the bottom boundary layer and strong upward motion through the tsunami-induced wave enhances significantly the particle transport to the surface. The energetic internal waves are capable of modifying the bathymetric shape of the shelf and continental slope in a similar manner as has been reported by internal tides (Cacchione *et al.* 2002) and by storms (Nittrouer and Wright 1994).

Fascinatingly, the wave patterns appear in all MODIS visible channels (figure 4), indicating a detection of an altered surface either by a change in the surface roughness or suspended sediment or both. The waves are seen in the VNIR channels (figure 5a) even at a lower resolution, but they are not evident in the TIR channels (figure 5c). For the visible channels, suspended sediment is well correlated with the apparent upwelling radiance, but this correlation diminishes toward the near infrared (the wavelength from 1000 to 3000 nm) (Currant and Novo 1988). Such a relationship has also been shown by Mobasheri and Mousavi (2004) with a decrease in the correlation between suspended sediment and reflectance for the longer near infrared wavelengths. Moreover, coarse material like sand found at the shelf of Sri Lanka is unlikely to stay resuspended for a long period of time (Kudraß; pers. comm.). Because of this, the signal seen in the near infrared channel (Figure 5 b) indicates that physical processes, like the interactions between internal wave-induced surface currents and surface waves, are detected. Significant alterations of the pycnocline and thermocline by internal waves may affect variations in the temperature near the sea surface (Farmer and Armi, 1999). However, the brightness temperature in the TIR (figure 5c) does not support strong variations in the sea surface temperatures.

In conclusion, the tsunami-induced wave patterns detected by MODIS are likely generated by internal waves, modified by interactions with surface waves, which result in changes in the surface roughness. It remains unclear, both theoretically and observationally, how these internal waves have substantially affected the suspended sediment concentration at the sea surface and how much these changes have affected the shelf break and continental slope. Thus, a clear understanding of vertical and horizontal mixing and its effect on the sediment transport is needed for future investigations.

An enhanced observational network including both measurements of physical as well as biogeochemical parameters in regions of high tsunami frequency would be required to understand the complexity of the internal waves and wave interactions generated by a tsunami in detail. These data, together with remote sensing data and a high-resolution bathymetry, could be assimilated into numerical models to investigate the wave pattern observed by satellite images. Such a test with existing models (e.g., Kowalik *et al.* 2005, Titov *et al.* 2005 <u>http://www.pmel.noaa.gov/tsunami/research.html</u>, <u>http://tsun.sscc.ru/tsulab/20041226.htm</u>, Farmer and Armi 1999) to explain these data will be a challenging and important task for the future and can contribute to an improved tsunami forecast by these models.

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Figure 1. A true colour image from MODIS over the eastern half of Sri Lanka and adjacent Indian Ocean. This is from 0510 GMT on 26 December 2004. The yellow box is a cloud-free region near Batticaloa where we looked for oceanic evidence of the tsunami. (Courtesy of Liam Gumley, Space Science and Engineering Center , University of Wisconsin-Madison).



Figure 2. Off the eastern coast of Sri Lanka. This is an enhanced, colour image using two visible channels (band 1 and 2) from the MODIS instrument from one week earlier (on the left) and less than 2.5 hours after tsunami hit on right. The range of reflected radiance over the ocean is about 6 watts m<sup>-2</sup> sr<sup>-1</sup> micron<sup>-1</sup>. The solar zenith angle is 36 degrees for both days. The distance from shore to the bow wave in the middle is about 16 km. The distance between waves is about 6 km.



Figure 3. The reflected radiance of figure 2 overlaid with contours of the bathymetry data. The bathymetry data is from the National Geophysical Data Center (NGDC). We used the ETOPO2 global 2-minute gridded elevation data interpolated and smoothed to match the higher resolution of the satellite data. The dashed contours are depths in meters.



Figure 4. The reflected radiance of three MODIS bands that compose the three-colour image in figure 3. From left to right they are band 1 (620 - 670 nm), band 4 (545 - 565 nm), band 3 (459 - 479 nm), corresponding to red, green, blue, respectively.



Figure 5. Left panel is reflected radiance of MODIS band 1 (620 – 670 nm, visible channel). Middle panel is the reflected radiance of band 6 (1628 – 1652 nm, near infrared). Right panel is the brightness temperature of band 31 (11000 nm, thermal infrared channel). This is 1 km data displayed at 250 m resolution.